# Trade, Education, and The Shrinking Middle Class

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#### Introduction

The Model A Tractable 2-Country Example Extensions Policy Analysis Concluding Remarks Motivation Stylized Facts Overview Roadmap Related Literature

# Motivation

#### Public perception at odds with trade models

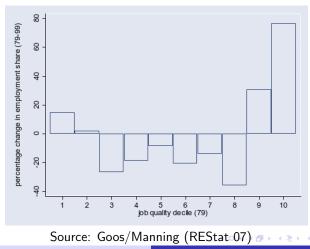
- Growing popular concern that the middle class is shrinking, likely due to globalization.
- Even those with a solid education no longer seem safe from losing jobs and social standing.
- At the same time, trade theory treats education crudely, most often as a binary variable.

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Introduction

The Model A Tractable 2-Country Example Extensions Policy Analysis Concluding Remarks Motivation Stylized Facts Overview Roadmap Related Literature

#### Stylized Facts: Polarization of Job Quality (U.K 1979-1999)

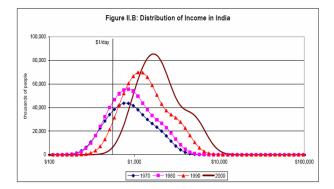


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Motivation Stylized Facts Overview Roadmap Related Literature

Stylized Facts: Expanding Middle Class (India 1970-2000)



Source: Sala-i-Martin (QJE 06)

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#### Introduction

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# Overview

#### Our approach:

- Continuum of sectors model with trade in intermediate goods/tasks and endogenous skill acquisition.
- Agents of different ability levels self-select into occupational sectors by acquiring the corresponding human capital.
- Countries differ in educational institutions resulting in a different educational cost structure ⇒ comparative advantage.
- Trade liberalization can (and generally will) lead to non-monotonic skill change within countries; welfare effects of trade typically non-monotonic; middle class may suffer most.

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#### Introduction

The Model A Tractable 2-Country Example Extensions Policy Analysis Concluding Remarks Motivation Stylized Facts Overview Roadmap Related Literature

# Roadmap

#### Outline of this talk:

- related literature
- the model
- a tractable example
- limited diversification
- policy analysis
- concluding remarks

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# Related Literature

Labor Literature: Documenting non-monotonic wage changes

 Autor/Levy/Murnane (QJE 03), Autor/Dorn (07), Goos/Manning (REStat 07), Falvey/Greenaway/Silva (08).

#### Trade Literature

- trade vs. technology: Krugman, Feenstra, and others;
- binary skill models: Blanchard/Willmann (08), and others;
- continuous sectors: Dornbusch/Fischer/Samuelson (AER 77, 80), Grossman/Rossi-Hansberg (08), Jim Anderson (08);
- heterogeneous firms and workers: Yeaple (JIE 05), Helpman/Itskhoki/Redding (08);
- similar results: Jung/Mercenier (08), Costinot/Vogel (09).

Model Set-up Solving the Model

## Model Set-up

#### Basics

- Two countries: Home and Foreign
- Population:
  - Heterogeneous agents; unit mass in each country
  - Agents differ in ability, indexed by  $a \in [0,1]$
  - Same ability distribution F(a) in both countries
- Intermediates:
  - Continuum of tradeable intermediate sectors/tasks:  $j \in [0,1]$
  - Identity production function in each sector  $\Rightarrow w(j) = p(j)$
- One final good, numeraire:
  - $Y = \psi(\vec{y})$  where  $\psi(\cdot)$  is hd 1 in intermediates.
  - Unit demand for intermediate  $j: x(j) \equiv x_j(\vec{w})$ .

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Model Set-up Solving the Model

### Model Set-up

#### Cost of Education

 Cost of education for agent a to enter sector j (measured in units of Y):

 $c(j,a) \in C^2$ 

where:

$$rac{\partial c(j,a)}{\partial j} > 0$$
  $rac{\partial c(j,a)}{\partial a} < 0$   
 $rac{\partial^2 c(j,a)}{\partial j \partial a} < 0$   $rac{\partial^2 c(j,a)}{\partial j^2} > 0.$ 

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• Less generally, let: c(j, a) = h(a)g(j)

Model Set-up Solving the Model

## Solving the Supply Side

#### **Optimal Sorting**

Agents solve

$$\max_j w(j) - c(j, a)$$

• FOC:

$$\frac{\partial c(j,a)}{\partial j} \equiv \dot{c}(j,a) = \dot{w}(j)$$

$$\Rightarrow a(j) = h^{-1}(\dot{w}/\dot{g})$$

• Lemma:  $a'(j) \ge 0$  as long as  $\dot{w}(j) > 0$ .

- Supply of intermediate good/task j is: y<sup>s</sup>(j) = a'(j)f(a(j))
- Output of final good is  $Y = \psi(\vec{y})$  where  $y(j) = y^s(j) + y_j^t$ .

Model Set-up Solving the Model

### Small Open Economy

• Take wage/price schedule as fixed w/  $w(j) \in C^1$ ,  $\dot{w}(j) > 0 \ \forall j$ .

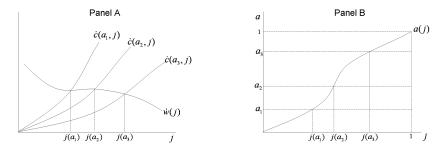


Figure: Monotonic Sorting across Occupations

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Model Set-up Solving the Model

## Non-Monotonic Skill Change in an SOE

• Consider an exogenous shift in wages from  $w^{o}(j)$  to  $w^{1}(j)$ .

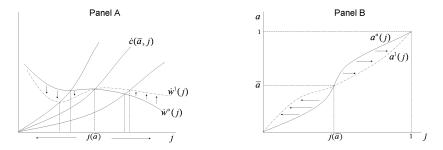


Figure: Low Ability Agents Sort Down; High Ability Sort Up

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Model Set-up Solving the Model

### General Equilibrium with Two Large Countries

Equilibrium Conditions (Free Trade):

• Full employment:

$$\int_0^1 a'(j)f(a(j))dj = 1; \qquad \int_0^1 a'^*(j)f(a^*(j))dj = 1$$

Zero profit:

$$1 = \int_0^1 w(j) x(j) dj; \qquad 1 = \int_0^1 w(j) x^*(j) dj$$

Balanced budget:

$$Y^{d} = \int_{0}^{1} [w(j(a)) - c(a, j(a))] da; \qquad Y^{d*} = \int_{0}^{1} [w(j^{*}(a)) - c(a, j^{*}(a))] da$$

• Market clearing in intermediates:

$$a'(j)f(a(j)) + a'^{*}(j)f(a^{*}(j)) = x(j)Y^{s} + x^{*}(j)Y^{s*} \forall j$$

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Model Set-up Solving the Model

### General Equilibrium Solution

#### Solution Strategy

• Characterize market clearing conditions as differential eq'n of w(j) using definition of a(j):

$$h^{-1\prime} \Big(\frac{\dot{w}}{\dot{g}}\Big) \Big[\frac{\dot{g}\ddot{w} - \ddot{g}\dot{w}}{\dot{g}^2}\Big] f\Big(h^{-1}\Big(\frac{\dot{w}}{\dot{g}}\Big)\Big) + h^{*-1\prime}\Big(\frac{\dot{w}}{\dot{g}^*}\Big) \Big[\frac{\dot{g}^*\ddot{w} - \ddot{g}^*\dot{w}}{\dot{g}^{*2}}\Big] f^*\Big(h^{*-1}\Big(\frac{\dot{w}}{\dot{g}^*}\Big)\Big) \\ = x(j)Y^s(\vec{w}) + x^*(j)Y^{*s}(\vec{w}),$$

which yields equilibrium wage schedule, w(j).

- Use w(j) to find equilibrium mapping functions a(j) and a\*(j) and supply schedules y(j), y\*(j).
- Finally, the balanced budget condition pins down final good output, consumption, and the pattern of trade.

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Assumptions Equilibrium prices Optimal Sorting, Human Capital Acquisition Welfare Analysis

# A Functional Form Example

#### Assumptions

- $a \sim U[0,1]$
- Cost structure:

$$c(j,a) = rac{1-a}{a} imes rac{2j^2}{5}$$
  
 $c^*(j,a) = rac{1-a}{a} imes rac{2j^3}{3}$ 

- Leontief final good production:
  - $\Rightarrow$  unit factor demand:  $x(j) = x^*(j) = 1$
  - $\Rightarrow$  price index (with Y as numeraire):  $1 = \int_0^1 w(j) dj$

#### Thought Experiment: Autarky $\rightarrow$ Free Trade

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### **Closed Form Solutions for Wage Gradients**

Using the functional form of the cost in the FOC's, and noting that Leontief implies a(j) = j or a'(j) = 1 under autarky, we obtain:

#### Autarky wage/price schedules

• 
$$\dot{w}_A(j) = \frac{4(1-j)}{5}$$

• 
$$\dot{w}^*_A(j) = 2j(1-j)$$

#### Free trade wage/price schedule

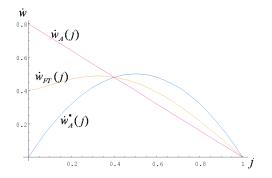
• 
$$\dot{w}_{FT}(j) = \frac{j(2+j-10j^2) + \sqrt{j^2(4+j(4+4j(121+20j(-9+5j))))}}{10j}$$

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### Comparing Autarky and Free Trade Wage Gradients



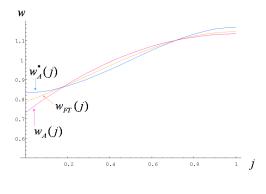
#### Slopes of the Equilibrium Wage Schedules

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## Equilibrium Wage/Price Schedule



Where 
$$w_0 = 1 - \int_0^1 \dot{w}(j) dj$$

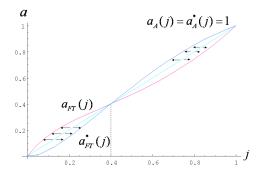
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### Ability-to-Sector Mappings



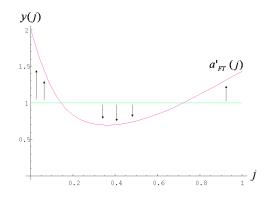
Non-Monotonic Skill Change at Home and Abroad

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### Change in Employment at Home



#### Shifting Sectoral and Educational Choices at Home: Vacating the Middle

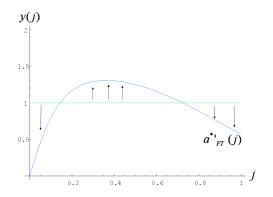
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### Change in Employment in Foreign



#### Shifting Sectoral and Educational Choices in Foreign: Expansion of Middle Sector Employment

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# Welfare Analysis

Two Components of Net Real Wages

For a given agent, a:

- Real wage: w(j(a))
- Real cost of education: c(j(a), a)

#### Net Real Welfare Change

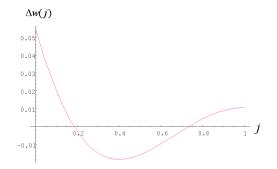
$$[w_{\mathsf{FT}}(j_{\mathsf{FT}}(\mathsf{a})) - w_{\mathsf{A}}(j_{\mathsf{A}}(\mathsf{a}))] - [c(j_{\mathsf{FT}}(\mathsf{a}), \mathsf{a}) - c(j_{\mathsf{A}}(\mathsf{a}), \mathsf{a})]$$

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### Change in the real wage in sector *j* Home



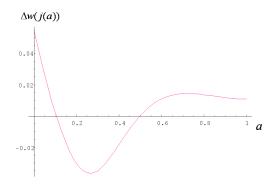
Change in Home's Real Wages by Sector

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### Change in the real wage of Home agent a



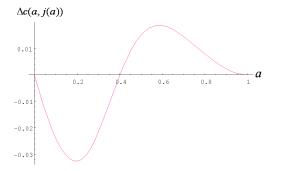
#### Change in Home's Real Wages by Agent

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### Change in the realized cost of education for Home workers



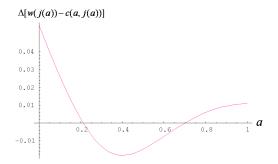
Change in the Cost of Education by Agent (Home)

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### Net Welfare Change for Home Workers

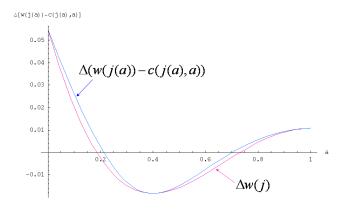


Middle Ability Agents Lose from Trade

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### Aside: A Short Run Perspective: Fixed Education Costs.

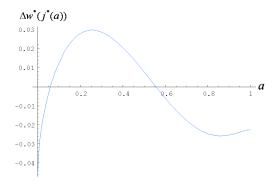


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### Foreign Real Wage Changes



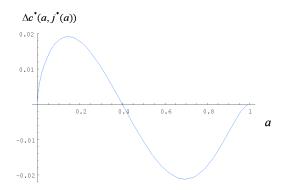
#### Change in the Foreign Real Wage by Agent

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### Foreign Real Cost of Education Changes



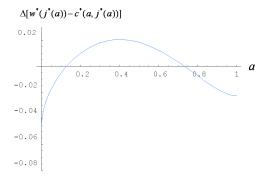
Change in the Cost of Education by Agent (Foreign)

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### Net Welfare Change for Foreign Workers



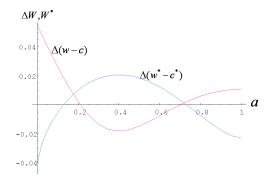
#### Net Welfare Gains Accrue to Middle Ability Agents

Introduction
The Model
A Tractable 2-Country Example
Extensions
Policy Analysis
Concluding Remarks

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#### Summary



#### Non-Monotonic Welfare Changes in Both Countries

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## Aggregate Gains from Trade

#### Magnitude of gains from trade

- Aggregate gains from trade for Home:
  - Real wages rise most in low *j* sectors, moderately in high *j* sectors, and fall in middle *j* occupations.
  - Real cost of education falls for low ability agents; rises for high ability.
  - ⇒ Welfare gains at upper and lower ends of ability distribution, losses in the middle.
- Aggregate gains for Foreign:
  - Real wages fall most in low *j* sectors, moderately in high *j* sectors, and rise for middle *j* occupations.
  - Real cost of education rises for lower ability agents and rises for high ability.
  - ⇒ Welfare losses at upper and lower ends of distribution; gains concentrated in the middle.

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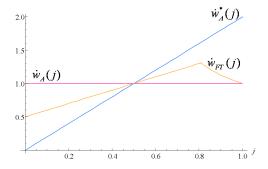
### Limited Diversification

- in the example countries stay diversified over the entire range
- are our results robust if that is not the case
- modified example with limited diversification under trade:

$$c[j,a] = \frac{1}{a} * \frac{j^2}{2}$$
  
 $c^*[j,a] = \frac{1}{a} * \frac{2j^3}{3}$ 

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### Wage Schedules with Limited Diversification

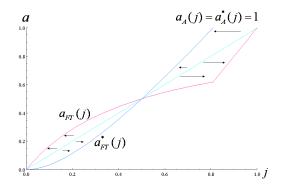


#### Wage Schedules under autarky and free trade

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### Aibility-Sector Mappings with Limited Diversification

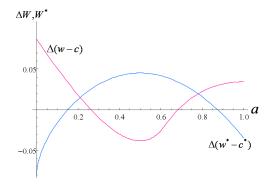


Ability-sector mappings under autarky and free trade

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### Net Welfare Effects under Limited Diversification



#### Net welfare effects of trade liberalization

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# **Educational Policy**

- such policy can take many possible forms
- we focus on educational subsidies
- augmented FOC:  $\dot{c}(j,a) \dot{s}(j) = \dot{w}(j)$
- same assumptions on c s as before on c
- Proposition:
  - if  $\dot{s} = 0$ , no effect
  - if  $\dot{s} > 0$ , sorting up
  - if  $\dot{s} < 0$ , sorting down
- to pop up middle class, target eg secondary education

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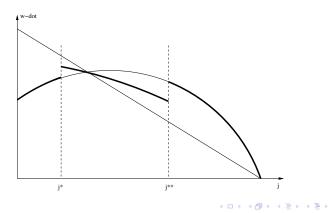


- very similar effects as educational policy
- FOC:  $\dot{c}(j, a) = \dot{w}(j) + \dot{t}(j)$
- effect depends on sign of  $\dot{t}$ :
  - if  $\dot{t} = 0$ , no effect
  - if  $\dot{t} > 0$ , sorting up
  - if  $\dot{t} < 0$ , sorting down
- but in addition distortion on demand side
- potentially beneficial if country can affect its terms of trade

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# Trade Policy

Suppose we want to soften the impact of globalization by (partially) off-setting the price shock for imports:



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# **Concluding Remarks**

- Education Policy and Comparative Advantage: Suggests more sophisticated strategies for targeting educational subsidies (i.e. primary, secondary, or tertiary levels and/or sector specific technical training)
- Political Economy: Suggests median voter may not be the average Joe more nuanced.
- Empirical Implications: Differentiating effect of trade on wages needs to account for endogeneity of workers' skill sets. Identification problem: measurability of ed. costs.
- Testability: Would like to see evidence of non-monotonic skill change for wide cross section of countries.

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# **Concluding Remarks**

#### Work in progress ...

- Further generalizing results
- Add differences in production technology to explore complementarity with ed. institutions.
- Non-traded goods/services
- Consider educational migration/outsourcing of education
- Use as stage game in dynamic political economy model
- Your suggestions welcome

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