Trade, Education, and The Shrinking Middle Class

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Introduction

The Model A Tractable 2-Country Example Extensions Policy Analysis Concluding Remarks Motivation Stylized Facts Overview Roadmap Related Literature

Motivation

Public perception at odds with trade models

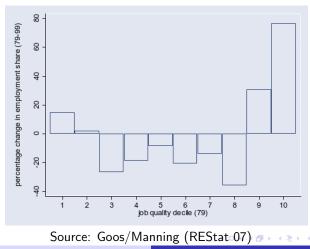
- Growing popular concern that the middle class is shrinking, likely due to globalization.
- Even those with a solid education no longer seem safe from losing jobs and social standing.
- At the same time, trade theory treats education crudely, most often as a binary variable.

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Stylized Facts: Polarization of Job Quality (U.K 1979-1999)

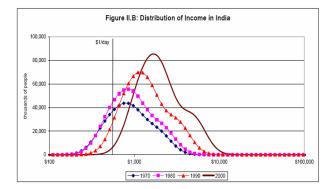


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Stylized Facts: Expanding Middle Class (India 1970-2000)



Source: Sala-i-Martin (QJE 06)

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Overview

Our approach:

- Continuum of sectors model with trade in intermediate goods/tasks and endogenous skill acquisition.
- Agents of different ability levels self-select into occupational sectors by acquiring the corresponding human capital.
- Countries differ in educational institutions resulting in a different educational cost structure ⇒ comparative advantage.
- Trade liberalization can (and generally will) lead to non-monotonic skill change within countries; welfare effects of trade typically non-monotonic; middle class may suffer most.

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Introduction

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Roadmap

Outline of this talk:

- related literature
- the model
- a tractable example
- limited diversification
- policy analysis
- concluding remarks

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Motivation Stylized Facts Overview Roadmap Related Literature

Related Literature

Labor Literature: Documenting non-monotonic wage changes

 Autor/Levy/Murnane (QJE 03), Autor/Dorn (07), Goos/Manning (REStat 07), Falvey/Greenaway/Silva (08).

Trade Literature

- trade vs. technology: Krugman, Feenstra, and others;
- binary skill models: Blanchard/Willmann (08), and others;
- continuous sectors: Dornbusch/Fischer/Samuelson (AER 77, 80), Grossman/Rossi-Hansberg (08), Jim Anderson (08);
- heterogeneous firms and workers: Yeaple (JIE 05), Helpman/Itskhoki/Redding (08);
- similar results: Jung/Mercenier (08), Costinot/Vogel (09).

Model Set-up Solving the Model

Model Set-up

Basics

- Two countries: Home and Foreign
- Population:
 - Heterogeneous agents; unit mass in each country
 - Agents differ in ability, indexed by $a \in [0,1]$
 - Same ability distribution F(a) in both countries
- Intermediates:
 - Continuum of tradeable intermediate sectors/tasks: $j \in [0,1]$
 - Identity production function in each sector $\Rightarrow w(j) = p(j)$
- One final good, numeraire:
 - $Y = \psi(\vec{y})$ where $\psi(\cdot)$ is hd 1 in intermediates.
 - Unit demand for intermediate $j: x(j) \equiv x_j(\vec{w})$.

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Model Set-up Solving the Model

Model Set-up

Cost of Education

 Cost of education for agent a to enter sector j (measured in units of Y):

 $c(j,a) \in C^2$

where:

$$rac{\partial c(j,a)}{\partial j} > 0$$
 $rac{\partial c(j,a)}{\partial a} < 0$
 $rac{\partial^2 c(j,a)}{\partial j \partial a} < 0$ $rac{\partial^2 c(j,a)}{\partial j^2} > 0.$

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• Less generally, let: c(j, a) = h(a)g(j)

Model Set-up Solving the Model

Solving the Supply Side

Optimal Sorting

Agents solve

$$\max_j w(j) - c(j, a)$$

• FOC:

$$\frac{\partial c(j,a)}{\partial j} \equiv \dot{c}(j,a) = \dot{w}(j)$$

$$\Rightarrow a(j) = h^{-1}(\dot{w}/\dot{g})$$

• Lemma: $a'(j) \ge 0$ as long as $\dot{w}(j) > 0$.

- Supply of intermediate good/task j is: y^s(j) = a'(j)f(a(j))
- Output of final good is $Y = \psi(\vec{y})$ where $y(j) = y^s(j) + y_j^t$.

Model Set-up Solving the Model

Small Open Economy

• Take wage/price schedule as fixed w/ $w(j) \in C^1$, $\dot{w}(j) > 0 \ \forall j$.

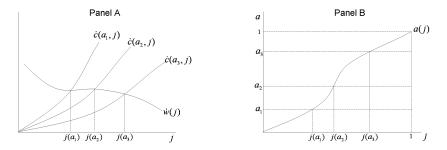


Figure: Monotonic Sorting across Occupations

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Model Set-up Solving the Model

Non-Monotonic Skill Change in an SOE

• Consider an exogenous shift in wages from $w^{o}(j)$ to $w^{1}(j)$.

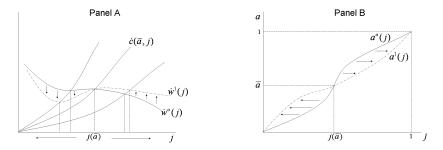


Figure: Low Ability Agents Sort Down; High Ability Sort Up

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Model Set-up Solving the Model

General Equilibrium with Two Large Countries

Equilibrium Conditions (Free Trade):

• Full employment:

$$\int_0^1 a'(j)f(a(j))dj = 1; \qquad \int_0^1 a'^*(j)f(a^*(j))dj = 1$$

Zero profit:

$$1 = \int_0^1 w(j) x(j) dj; \qquad 1 = \int_0^1 w(j) x^*(j) dj$$

Balanced budget:

$$Y^{d} = \int_{0}^{1} [w(j(a)) - c(a, j(a))] da; \qquad Y^{d*} = \int_{0}^{1} [w(j^{*}(a)) - c(a, j^{*}(a))] da$$

• Market clearing in intermediates:

$$a'(j)f(a(j)) + a'^{*}(j)f(a^{*}(j)) = x(j)Y^{s} + x^{*}(j)Y^{s*} \forall j$$

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Model Set-up Solving the Model

General Equilibrium Solution

Solution Strategy

• Characterize market clearing conditions as differential eq'n of w(j) using definition of a(j):

$$h^{-1\prime} \Big(\frac{\dot{w}}{\dot{g}}\Big) \Big[\frac{\dot{g}\ddot{w} - \ddot{g}\dot{w}}{\dot{g}^2}\Big] f\Big(h^{-1}\Big(\frac{\dot{w}}{\dot{g}}\Big)\Big) + h^{*-1\prime}\Big(\frac{\dot{w}}{\dot{g}^*}\Big) \Big[\frac{\dot{g}^*\ddot{w} - \ddot{g}^*\dot{w}}{\dot{g}^{*2}}\Big] f^*\Big(h^{*-1}\Big(\frac{\dot{w}}{\dot{g}^*}\Big)\Big) \\ = x(j)Y^s(\vec{w}) + x^*(j)Y^{*s}(\vec{w}),$$

which yields equilibrium wage schedule, w(j).

- Use w(j) to find equilibrium mapping functions a(j) and a*(j) and supply schedules y(j), y*(j).
- Finally, the balanced budget condition pins down final good output, consumption, and the pattern of trade.

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Assumptions Equilibrium prices Optimal Sorting, Human Capital Acquisition Welfare Analysis

A Functional Form Example

Assumptions

- $a \sim U[0,1]$
- Cost structure:

$$c(j,a) = rac{1-a}{a} imes rac{2j^2}{5}$$

 $c^*(j,a) = rac{1-a}{a} imes rac{2j^3}{3}$

- Leontief final good production:
 - \Rightarrow unit factor demand: $x(j) = x^*(j) = 1$
 - \Rightarrow price index (with Y as numeraire): $1 = \int_0^1 w(j) dj$

Thought Experiment: Autarky \rightarrow Free Trade

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Closed Form Solutions for Wage Gradients

Using the functional form of the cost in the FOC's, and noting that Leontief implies a(j) = j or a'(j) = 1 under autarky, we obtain:

Autarky wage/price schedules

•
$$\dot{w}_A(j) = \frac{4(1-j)}{5}$$

•
$$\dot{w}^*_A(j) = 2j(1-j)$$

Free trade wage/price schedule

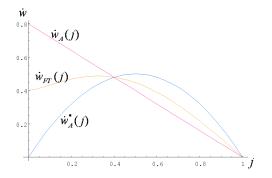
•
$$\dot{w}_{FT}(j) = \frac{j(2+j-10j^2) + \sqrt{j^2(4+j(4+4j(121+20j(-9+5j))))}}{10j}$$

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Comparing Autarky and Free Trade Wage Gradients



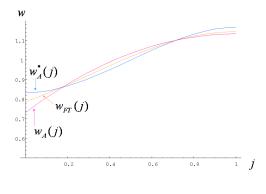
Slopes of the Equilibrium Wage Schedules

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Equilibrium Wage/Price Schedule



Where
$$w_0 = 1 - \int_0^1 \dot{w}(j) dj$$

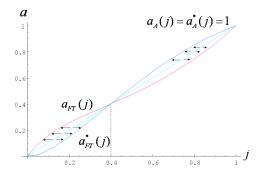
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Ability-to-Sector Mappings



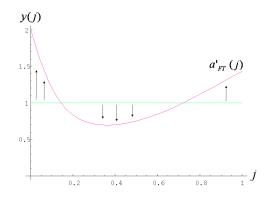
Non-Monotonic Skill Change at Home and Abroad

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Change in Employment at Home



Shifting Sectoral and Educational Choices at Home: Vacating the Middle

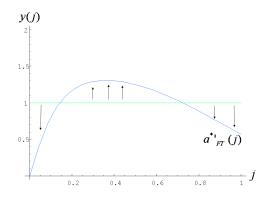
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Change in Employment in Foreign



Shifting Sectoral and Educational Choices in Foreign: Expansion of Middle Sector Employment

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Welfare Analysis

Two Components of Net Real Wages

For a given agent, a:

- Real wage: w(j(a))
- Real cost of education: c(j(a), a)

Net Real Welfare Change

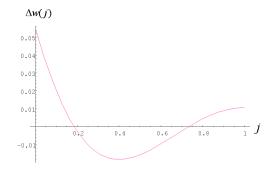
$$[w_{\mathsf{FT}}(j_{\mathsf{FT}}(\mathsf{a})) - w_{\mathsf{A}}(j_{\mathsf{A}}(\mathsf{a}))] - [c(j_{\mathsf{FT}}(\mathsf{a}), \mathsf{a}) - c(j_{\mathsf{A}}(\mathsf{a}), \mathsf{a})]$$

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Change in the real wage in sector *j* Home



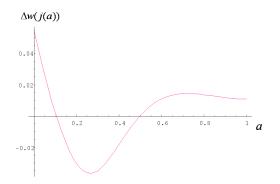
Change in Home's Real Wages by Sector

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Change in the real wage of Home agent a



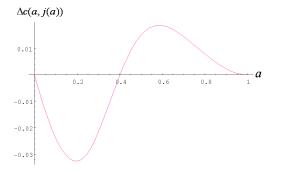
Change in Home's Real Wages by Agent

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Change in the realized cost of education for Home workers



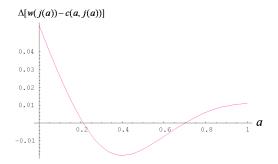
Change in the Cost of Education by Agent (Home)

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Net Welfare Change for Home Workers

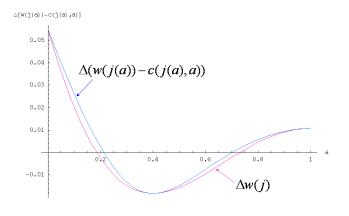


Middle Ability Agents Lose from Trade

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Aside: A Short Run Perspective: Fixed Education Costs.

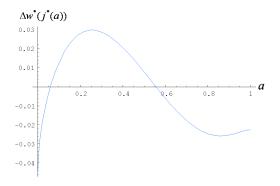


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Foreign Real Wage Changes



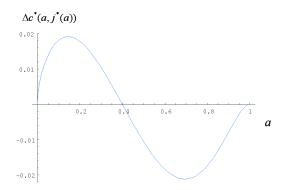
Change in the Foreign Real Wage by Agent

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Foreign Real Cost of Education Changes



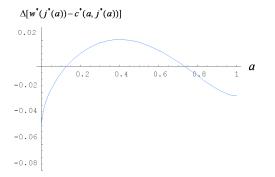
Change in the Cost of Education by Agent (Foreign)

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Net Welfare Change for Foreign Workers



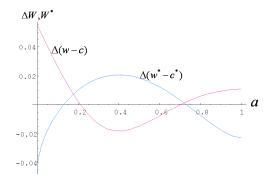
Net Welfare Gains Accrue to Middle Ability Agents

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Summary



Non-Monotonic Welfare Changes in Both Countries

Assumptions Equilibrium prices Optimal Sorting, Human Capital Acquisition Welfare Analysis

Aggregate Gains from Trade

Magnitude of gains from trade

- Aggregate gains from trade for Home:
 - Real wages rise most in low *j* sectors, moderately in high *j* sectors, and fall in middle *j* occupations.
 - Real cost of education falls for low ability agents; rises for high ability.
 - ⇒ Welfare gains at upper and lower ends of ability distribution, losses in the middle.
- Aggregate gains for Foreign:
 - Real wages fall most in low *j* sectors, moderately in high *j* sectors, and rise for middle *j* occupations.
 - Real cost of education rises for lower ability agents and rises for high ability.
 - ⇒ Welfare losses at upper and lower ends of distribution; gains concentrated in the middle.

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Limited Diversification

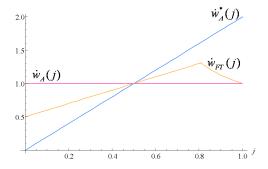
- in the example countries stay diversified over the entire range
- are our results robust if that is not the case
- modified example with limited diversification under trade:

$$c[j,a] = \frac{1}{a} * \frac{j^2}{2}$$

 $c^*[j,a] = \frac{1}{a} * \frac{2j^3}{3}$

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Wage Schedules with Limited Diversification

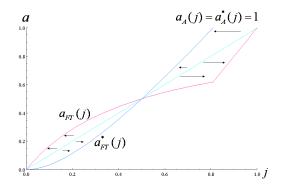


Wage Schedules under autarky and free trade

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Aibility-Sector Mappings with Limited Diversification

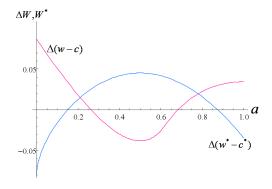


Ability-sector mappings under autarky and free trade

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Net Welfare Effects under Limited Diversification



Net welfare effects of trade liberalization

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Educational Policy

- such policy can take many possible forms
- we focus on educational subsidies
- augmented FOC: $\dot{c}(j,a) \dot{s}(j) = \dot{w}(j)$
- same assumptions on c s as before on c
- Proposition:
 - if $\dot{s} = 0$, no effect
 - if $\dot{s} > 0$, sorting up
 - if $\dot{s} < 0$, sorting down
- to pop up middle class, target eg secondary education

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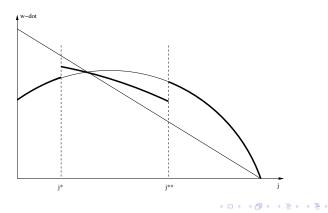


- very similar effects as educational policy
- FOC: $\dot{c}(j, a) = \dot{w}(j) + \dot{t}(j)$
- effect depends on sign of \dot{t} :
 - if $\dot{t} = 0$, no effect
 - if $\dot{t} > 0$, sorting up
 - if $\dot{t} < 0$, sorting down
- but in addition distortion on demand side
- potentially beneficial if country can affect its terms of trade

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Trade Policy

Suppose we want to soften the impact of globalization by (partially) off-setting the price shock for imports:



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Concluding Remarks

- Education Policy and Comparative Advantage: Suggests more sophisticated strategies for targeting educational subsidies (i.e. primary, secondary, or tertiary levels and/or sector specific technical training)
- Political Economy: Suggests median voter may not be the average Joe more nuanced.
- Empirical Implications: Differentiating effect of trade on wages needs to account for endogeneity of workers' skill sets. Identification problem: measurability of ed. costs.
- Testability: Would like to see evidence of non-monotonic skill change for wide cross section of countries.

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Concluding Remarks

Work in progress ...

- Further generalizing results
- Add differences in production technology to explore complementarity with ed. institutions.
- Non-traded goods/services
- Consider educational migration/outsourcing of education
- Use as stage game in dynamic political economy model
- Your suggestions welcome

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